

The Islamic Science of Weights and Balances: A Refoundation of Mechanics Deeply Rooted in the Social Context of the Islamic Civilization

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THE ISLAMIC SCIENCE OF WEIGHTS AND BALANCES: A REFOUNDATION OF MECHANICS DEEPLY ROOTED IN THE SOCIAL CONTEXT OF THE ISLAMIC CIVILIZATION

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Three¹ main concerns are focused upon in the following article. The first is an overview of the textual tradition of a core-part of Arabic mechanics dealing with the science of weights. Then the historical significance of the Arabic science of weights is analyzed. Thus, the transformation brought about by this important segment of Arabic mechanics is interpreted as the reorganization of a core-part of ancient mechanics into an independent science of weights. On this basis, a strong claim is made in favor of the independent status of *ʿilm al-athqāl*, which should no longer be confused with *ʿilm al-úyyāl*, understood as a general descriptive discourse on different types of machines. The final section is devoted to a preliminary survey of the institutional setting of the control of weighing instruments in the Islamic medieval society through the office of the *úisba*. This study, covering the theoretical as well as the practical aspects of an important segment of Arabic classical science, i.e. mechanics, is part of a program of research which the author is developing, appealing for the renewal of the field of the history of Arabic classical sciences, by merging together historical research based on empirical investigation in the scientific texts, the epistemological reflexion on the concepts, categories and methods, and the sociological analysis of the contextual structures that shaped the practice of science in medieval Islam.²

The reconstruction of the corpus of the Arabic science of weights

The balance is an instrument of our current life, charged with history and science. In Islamic classical times, this familiar instrument was the object of an extensive scientific and technical debate of which dozens of treatises on different aspects of its theory, construction, and use are the precious remains. Different sorts of balances were the object of such an extensive enquiry, including the normal equal-armed balance (called in Arabic *mázzān*, *ʿayyān*, and *shāhān*), the steelyard (called *qarasʿīn*, *qaffān*, and *qabbān*) and sophisticated balances for weighing absolute and specific weights of substances.

¹ An earlier version of this article was published in Abattouy 2002b. Several results exposed in this study were obtained under the sponsorship of the Max Planck Institute for the History of Science (MPIWG) in Berlin (1996-2003). I am grateful to my colleagues at the MPIWG, especially to Professor Jürgen Renn, director of Department I at the MPIWG, for this long-lasting and fruitful collaboration.

² For case studies, reflexions and references bringing evidence to this research program, see the three forthcoming volumes: Abattouy [In Press 2006a], [In Press 2006b], and [In Press 2006c]

Several drawings of balances are preserved in Arabic manuscripts, such as those of al-Kh zin , al-  ar r , and al-Qazw n . Further, some specimens of the ancient balances survived and are presently kept in museums. For illustration, we refer to two such Islamic steelyards from the 10th-12th centuries. The first, built in Iran, is preserved in the National Museum in Kuwait (LNS 65M). It is made of steel, bears marks on its beam. Its dimensions (height: 11.5 cm, length: 15.6 cm) show that it was used for weighing small quantities.³ The second is kept in the Science Museum in London (accession number Inv. 1935-457). This balance came to the Science Museum in 1935 from the University College in London, together with a large selection of archaeological material consisting of ancient weights and measures collected from the Near East by the British archaeologist Flinders Petrie. A scale of silver is inlaid along its 2.37m long, wrought-iron beam. It bears two suspending elements and corresponding calibrations: one ranging from 0 to 900 *ra l*-s (1 *ra l* is approximately 1 pound); the other ranging from 900 to 1820 *ra l*-s.⁴

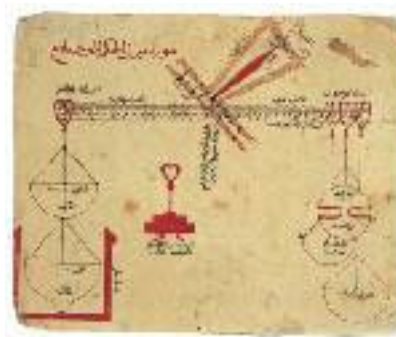


Figure 1. Al-Kh zin 's balance, in Al-Kh zin , *Kit b m z n al- ikma*, Hyderabad, 1940 (The image was introduced by the editor).

The interest in the balance in Islamic scientific learning was culturally nurtured by its role as a symbol of good morals and justice. The Qur n and the   ad th appealed extensively to a strict observance of fair and accurate weighing practices with the balance. Considered the tongue of justice and a direct gift of God, the balance was made a pillar of the right society and a tool of good governance. These principles were recorded explicitly in several treatises on the balance, such as the introduction to *Kit b m z n al- ikma* by al-Kh zin , where the balance is qualified as "the tongue of justice and the article of mediation." Furthermore, it was counted as a fundamental factor of justice, on the same level with "the glorious Book of God," and "the guided leaders and established savants."⁵

The emergence of Arabic mechanics is an early achievement in the scientific tradition of Islam. Actually, already in the mid-9th century, and in close connection with the translation of Greek texts into Arabic, treatises on different aspects of the mechanical arts were composed in Arabic, but with a marked focus on balances and weights. These writings, composed by scientists as well as by mechanics and skilful artisans, gave birth to a scientific tradition with theoretical and practical aspects, debating mathematical

³ See al- ab   1989, p. 32.

⁴ The images of these balances can be seen at http://www.mpiwg-berlin.mpg.de/en/forschung/projects/theoreticalMechanics/project_image_Fig.11.jpg/showImagen and in Abattouy 2002b, p. 110.

⁵ Al-Kh zin  1940, pp. 3-4.

and physical problems, and involving questions relevant to both the construction of instruments and the social context of their use. Some of these Arabic treatises were translated into Latin in the 12th century and influenced the European science of weights.

The corpus of the Arabic science of weights covers the entire temporal extent of scientific activity in medieval Islam and beyond, until the 19th century. The reasons for such an abundance of literature on the problems of weighing can be explained only by contextual factors. In fact, the development of the science of weights as an autonomous branch of science was triggered by the eminent importance of balances for commercial purposes. In a vast empire with lively commerce between culturally and economically fairly autonomous regions, more and more sophisticated balances were, in the absence of standardization, key instruments governing the exchange of currencies and goods, such as precious metals and stones. It is therefore no surprise that Muslim scholars produced numerous treatises specifically dealing with balances and weights, explaining their theory, construction and use. This literature culminated in the compilation by >Abd ar-Raúmæn al-KhÆzinÿ, around 1120, of *KitÆb mÿzæn al-úikma*, an encyclopedia of mechanics dedicated to the description of an ideal balance conceived as a universal tool of a science at the service of commerce, the so-called 'balance of wisdom.' This was capable of measuring absolute and specific weights of solids and liquids, calculating exchange rates of currencies, and determining time.

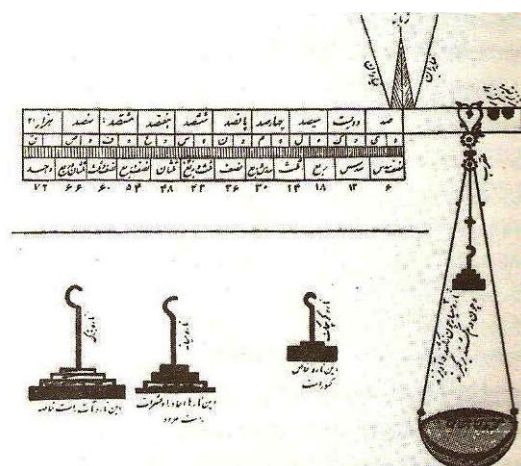


Figure 2. Al- KhÆzinÿ's balance, in Seyyed Hossein Nasr, *Islamic Science an Illustrated Study*, Kent 1976
 (The image was introduced by the editor).

A complete reconstruction of the Arabic tradition of weights is currently being undertaken by the author. This project began in the context of a long-term cooperation with the Max Planck Institute for the History of Science in Berlin. The work on the establishment of the Arabic corpus of the science of weights started in Fall 1996 by the systematic reconstruction of the entire codicological tradition of the corpus of texts dealing –on theoretical and practical levels– with balances and weights. By now almost two-thirds of the entire corpus has been edited and translated into English; this part, including texts dating from the 9th through the 12th centuries, is being prepared for publication with the appropriate commentaries.

The preliminary analysis of the texts investigated so far established the importance of the Arabic tradition for the development of the body of mechanical knowledge. The Arabic treatises turned out to be much

richer in content than those known from the ancient tradition. In particular, they contain foundations of deductive systems of mechanics different from those inferred from extant Greek texts, as well as new propositions and theorems. On the other hand, the Arabic treatises also represent knowledge about practical aspects of the construction and use of balances and other machines missing in ancient treatises.

The first phase of the research on the Arabic science of weights was focused on establishing the scope of its extant corpus. Surprisingly, this corpus turned out to be much larger than usually assumed in history of science. Up to now more than thirty treatises dating from the 9th through the 19th centuries have been identified which deal with balances and weights in the narrow sense. The majority of these treatises has never before been edited or studied, and only exists in one or more manuscript copies. Some important manuscripts have been discovered or rediscovered even in the course of the research activities conducted by the author.

The textual constituents of the Arabic works on the problems of weights can be classified chronologically into three successive units. First a set of Greek texts of mechanics extant in Arabic versions. Despite their Greek origin, these works can be regarded as an integral part of the Arabic mechanical tradition, at least because of the influence they exerted on the early works of Arabic mechanics. In the case of some of these texts, although they are attributed to Greek authors, their Greek originals are no more extant nor are they ascribed to their supposed Greek authors in antique sources. The second unit comprises founding texts composed originally in Arabic in the period from the 9th through the 12th centuries. This segment of writings laid the theoretical basis of the new science of weights, in close connection with the translations and editions of texts stemming from Greek origins. The third phase covers the 14th through the 19th centuries, and comprises mainly practical texts elaborating on the theoretical foundations laid in the earlier tradition. In the following, the texts belonging to these three phases will be described in brief, with a short characterization of some theoretical contents.

2. Arabic versions of Greek texts of mechanics

The corpus of Greek texts that were known to Muslim scholars through direct textual evidence and dealing with the problems of weighing and the theory of the balance are six in number:

1. First, *Nutaf min al-úyyal*, an Arabic partial epitome of Pseudo-Aristotle's *Mechanical Problems*: The *Problemata Mechanica*, apparently the oldest preserved text on mechanics, is a Greek treatise ascribed to Aristotle, but composed very probably by one of his later disciples. It has long been claimed that this text was not transmitted to Arabic culture. It is possible now to affirm that the scholars of Islamic lands had access to it at least through a partial epitome entitled *Nutaf min al-úyyal* (elements/extracts of mechanics) included by al-Kh  zin   in the fifth book of his *Kit  b m  z  n al-  ikma*.⁶

2-3. Two texts ascribed to Euclid on the balance (*Maq  la f   'l-m  z  n*) and on heaviness and lightness (*Kit  b fi 'l-thiqal wa 'l-khiffa*): Extant only in Arabic, the first one provides a geometrical treatment of the balance and presents a sophisticated demonstration of the law of the lever. It is not recorded if it was

⁶ Al-Kh  zin   1940, pp. 99-100. The text of the *Nutaf* was edited and translated, with commentaries, in Abattouy 2001a.

edited in Arabic, but there is enough evidence to conclude that this was probably the case. The second text survived in a version edited by ThĒbit ibn Qurra. It is an organized exposition –in 9 postulates and 6 theorems– of dynamical principles of the motion of bodies in filled media, developing a rough analysis of Aristotelian type of the concepts of place, size, kind and force and applying them to movements of bodies.⁷

4. A partial Arabic version of Archimedes' *On Floating Bodies*: Contrary to the highly creative impact Archimedes had on Arabic mathematics, it seems that his main mechanical treatises such as *Equilibrium of planes* and *Quadrature of the parabola* were not translated into Arabic. However, some elements of his theory of centers of gravity were disclosed in the mechanical texts of Heron and Pappus, whereas the main ideas of his hydrostatics were transmitted in a *MaqĒla fĒ 'l-thiqĒ wa 'l-khiffa*, extant in Arabic in several manuscript copies. This short tract consists in a summarized digest of the treatise on the *Floating Bodies*, presenting mere statements of the postulates and propositions of Book I and the first proposition of Book II without proofs.⁸

5.6. Heron's and Pappus' *Mechanics* : Finally, the last two Greek texts to be connected with the Arabic tradition of the science of weights are the two huge treatises referred to as *Mechanics* of the Alexandrian scholars Heron (1st century) and Pappus (4th century). These texts are together major sources for the reconstruction of the history of ancient mechanical ideas. Given their composite character, only some of their chapters concern the foundations of theoretical mechanics as developed in the later Arabic tradition around the questions of weighing. Heron's *Mechanics* was translated into Arabic by QusĒ ibn LĒqĒ under the title *FĒ rafĒ al-ashyĒ al-thaqĒla* (On lifting heavy loads).⁹ After the loss of the Greek original text, it survived only in this Arabic version. On the contrary of Heron's *Mechanics*, Pappus mechanical treatise was preserved in Greek and in Arabic. Its Arabic version is titled *Madkhal ilĒ ilĒm al-ūiyal* (Introduction to the science of mechanics), by a translator who has not yet been identified, but there is enough evidence to affirm that this version saw the light in 10th-century Baghdad.¹⁰

3. Founding texts of the Arabic science of weights

In close connection with the translation and study of the above mentioned Greek sources, the Muslim scientists composed in the period from the 9th up to the 12th century a set of original texts that laid the foundation to the new science of weights. To mention just the main treatises, these texts are seven in number:

7. First, the *KitĒb fĒ 'l-qarasĒn* by ThĒbit ibn Qurra (d. 901): Without contest the most important text of the Arabic mechanical tradition, it was apparently one of the first Arabic texts to deal with the theory of the unequal-armed balance in Islam and to systematize its treatment. As such, it established the theoretical foundation for the whole Arabic tradition.

⁷ The contents of these two works are surveyed in Abattouy 2001b, p. 216ff. Their textual tradition is analyzed under the procedure of *isĒlĒ* in Abattouy 2004c.

⁸ A MS copy of this text was published in Zotenberg 1879 and translated into English in Clagett 1959, pp. 52-55.

⁹ Heron's *Mechanics* was edited and translated twice respectively by Carra de Vaux in 1893, with French translation, and by Schmidt and Nix in 1900, with German translation. These editions were reprinted recently: respectively Herons 1976 and HĒron 1988.

Kitāb fī 'l-qaras' n presents a deductive theory of the steelyard based on dynamic assumptions. It is extant in four known copies, of which three contain complete texts with variant readings. Two of these, preserved in London (India Office MS 767-7) and Beirut (St.-Joseph Library, MS 223-11), were studied and published recently.¹¹ The third copy, formerly conserved in Berlin (Staatsbibliothek MS 559/9, ff. 218b-224a), was reported lost at the end of World War II. A colleague from Berlin, Paul Weinig and I happened to rediscover it in the Biblioteka Jagiellonska in Krakow (Poland) in October 1996. Recently Sonja Brentjes kindly attracted my attention over a partial fourth copy that exists in the archives of the Laurentiana Library in Florence (MS Or. 118, ff. 71r-72r). Never mentioned before, this valuable three-page text includes the introductory two sections of Thābit's treatise. This part of the text exposes the dynamic foundation of the treatise and an important passage that was thought of up to now to occur only in Beirut MS copy (and thus known as Beirut scholium).¹²

8. *Kitāb fī šifat al-wazn* by the same Thābit ibn Qurra: This five-section text on the balance is about the conditions necessary to achieve equilibrium in weighing with balances, primarily the equal-armed sort.¹³ An important connection between this text and *Kitāb fī 'l-qaras' n* is provided by the occurrence, in the last section of *šifat al-wazn*, of the statement of a proposition identical with the postulate that opens *Kitāb fī 'l-qaras' n*.

9. *Ziyyāda fī 'l-qaras' n* or An Addition on the theory of the *qaras' n*: A short anonymous text extant in a unicum copy preserved in Beirut. In this codex, the *Ziyyāda* serves as an appendix to *Kitāb fī 'l-qaras' n*. The two texts are written in the same hand and display strong terminological affinities which include the basic vocabulary as well as the technical terms. Thābit ibn Qurra is mentioned twice in the *Ziyyāda*. This and several other elements induce us to consider it as an appendix intended to amplify the analysis developed in Thābit's original work. The text of the *Ziyyāda* is composed of five propositions. The first two are mere applications of the Proposition VI of *Kitāb fī 'l-qaras' n* while the last three establish a procedure for calculating the counterweight required to maintain equilibrium in a lever divided an evenly number of times.

10. A short text on the balance by Mu'ammad ibn 'Abd-Allāh b. Manšūr al-Ahwāzī : Al-Ahwāzī is a well known mathematician of the 10th century; his text on the balance is extant in a unique copy preserved in Khuda Baksh Library in Patna (Codex 2928, folio 31) without title, save for the one provided by the curators of the library: *Risāla fī 'l-m'zān*.¹⁴

11. The treatises on centers of gravity of al-Qāhī and Ibn al-Haytham : These important contributions by two most important Muslim mathematicians of the 10th-11th centuries survived only through their

¹⁰ The Arabic text of Pappus' *Mechanics* was transcribed and translated into English in Jackson 1970.

¹¹ Respectively in Jaouiche 1976 and Knorr 1982.

¹² The mechanical theory of *Kitāb fī 'l-qaras' n* was studied in Jaouiche 1976, Abattouy 2000d and in Abattouy 2002a.

¹³ This text was preserved thanks to its integration in *Kitāb m'zān al-ūikma*: al-Khāzinī 1940, pp. 33-38. For translations, see the German version in Wiedemann 1970, vol. I, pp. 495-500 and a partial English version in Knorr 1982, pp. 206-208.

¹⁴ On al-Ahwāzī, see Sezgin 1974, p. 312.

reproduction by al-Kh  zin  in a joint abridged version that opens the first book of his *Kit b m z n al- ikma*.¹⁵ The potential discovery of the complete versions of these texts will mean the recovery of fundamental sources.¹⁶

12. The statements on the law of the lever by the same al-Q  h  included in a discussion on the centers of gravity he had with Ab  Is  q al-  b  around 990-91.¹⁷

13. The treatise of  ly  al-Ma r n on measures and weights:  ly  al-Ma r n was the Archbishop of Nisibin (north Mesopotamia) in the first half of the 11th century. His *Maq la f  'l-mak yy  wa al-awz n* (Treatise of measures and weights) is essentially of practical interest, but it is based on the theory of the steelyard as elaborated in earlier Arabic works.

14. *Irsh d dhaw  al- irf n il   in at al-qaff n* (Guiding the Learned Men in the Art of the Steelyard) by al-Isfiz r  : A fundamental and long-neglected treatise, written by Ab   tim al-Mu affar b. Ism  l al-Isfiz r , a mathematician and mechanic who flourished in Khuras n (north-east Iran) around 1050-1110. In this original text on the theory and practice of the unequal-armed balance, different textual traditions from Greek and Arabic sources are compiled together for the elaboration of a unified mechanical theory. It is extant in a unique manuscript copy preserved in Damascus (al- Asad National Library, al-  hiriyya collection, MS 4460, folii 16a-24a). In addition, an abridged version reproduced by al-Kh  zin  includes a section on the construction and use of the steelyard, which is omitted from the Damascus manuscript.¹⁸

15. *Kit b m z n al- ikma* by al-Kh  zin : A special mention should be made of *Kit b m z n al- ikma*, the encyclopedia of mechanics completed by Abderra m n al-Kh  zin  in 1121-22, a real mine of information on all aspects of the theoretical and practical knowledge in the Islamic medieval area about balances. The book covers a wide range of topics related to statics, hydrostatics, and practical mechanics, besides reproducing abridged editions of several mechanical texts by or ascribed to Greek and Arabic authors. This huge summa of mechanical thinking provides a comprehensive picture of the knowledge about weights and balances available in the Arabic scientific milieu up to the early 12th century. Therefore, it represents a major source for any investigation on ancient and medieval mechanics.¹⁹

The textual tradition of the Arabic science of weights between the 9th and the 12th centuries also contains additional sources that should be taken into account in any complete reconstruction of its corpus. These

¹⁵ Al-Kh  zin  1940, pp. 15-20.

¹⁶ In his catalogue of Arabic manuscripts, Paul Sbath mentioned that there was a copy of Ibn al-Haytham's *Maq la f  'l-qaras n* in a private collection in Aleppo in Syria, which may be Ibn al-Haytham's treatise on centers of gravity: See Sbath 1938-1940, part 1, p. 86. For textual considerations on the treatise of al-Q  h , see Bancel 2001.

¹⁷ The correspondence was edited and translated into English in Berggren 1983.

¹⁸ al-Kh  zin  1940, pp. 39-45. Al-Isfiz r 's biography and the contents of his *Irsh d* are surveyed in Abattouy 2000b and Abattouy 2001b.

¹⁹ On al-Kh  zin  and his work, see Hall 1981 and Abattouy 2000a.

include the work of Mu'ammad Ibn Zakariyya al-Ra'zi (865-923) on the natural balance,²⁰ extracts from texts on weights by Qus' ibn L'iq and Is'eq ibn 'unayn,²¹ Ibn al-Haytham's largely expanded recension of Menelaus' (fl. Alexandria, 1st century) text on specific gravities,²² and two writings on specific gravity and the hydrostatical balance by 'Umar al-Khayy'm.²³

4. Texts of the later period

The third and last phase of the Arabic writings on weights and balances is represented by a group of texts dating from the 14th to the 19th century and originating principally from Egypt and Syria. These two countries were unified during this long period under the rule of the Ayy'bid, Mamel'k, and Ottoman dynasties, respectively, and they constituted for centuries a common economic and cultural space. Whence the *raison d'être* of this large amount of writings on the theoretical and practical problems of the balance and weights, since it was a direct outcome of the integration of economic and cultural activities in this vast area. The authors of these texts are mathematicians, mechanics, and artisans. In the following some names and works are mentioned for illustration.

16. *Mas'el fi 'l-maw'zin* (Problems on balances) by Ya'sh b. Ibr'h'm al-Umaw': This short tract is by a mathematician of Andalusian origin who lived in Damascus (fl. 1373), and is known as author of several arithmetical works.²⁴ His *Mas'el* consists in a small collection of problems about weighing with hydrostatic and normal balances. The text is part of the codex DR 86 preserved in the Egyptian National Library in Cairo.

17. *Ris'ala fi 'amal al-m'zin al-'ab'* by Taq' al-D'n ibn Ma'r'f: The author is a well known mathematician, astronomer, and mechanic (born in Damascus in 1525-died in Istanbul in 1585). His short treatise on making the natural balance describes what was transmitted to Taq' al-D'n of a previous writing on the balance that he ascribes to the mathematician Ghiyy'eth al-D'n al-K'esh' (died in Samarkand in 1429). It is part of the collections of the municipal library of Alexandria.

18. *'Amal m'zin li-sarf al-dhahab min ghayr sanj* (The construction of a balance for converting gold without standard weight) by Ab' 'l-'Abb'Es A'umad b. Ab' Bakr b. 'Al' ibn al-Sarr'ej. The author, who was alive around 714 H (1319-20) and 748 H (1347-8), was an important specialist of astronomical instrumentation in the Mamluk period.²⁵ His short text is the sixth item of the codex MR 30 conserved in the Egyptian National Library in Cairo.

²⁰ Reproduced in an abridged version by al-Kh'zin' 1940, pp. 83-86.

²¹ These texts are preserved in Aya Sofya Library in Istanbul, Codex 3711.

²² Obviously extant in a unique manuscript discovered in Lahore in 1979 by Anton Heinen: see Heinen 1983.

²³ Both edited in al-Kh'zin' 1940, pp. 87-92, 151-153. On Khayy'm's mechanics, see Aghayani Chavoshi and Bancel 2000, and Abbattouy 2005b.

²⁴ On al-Umaw', see Sa'd' 1981.

²⁵ See on Ibn al-Sarr'ej King 1987 and Charette 2003.

The Egyptian astronomer Muáammad ibn Abŷ al-Fatú al-ê´fŷ (d. 1543) composed several treatises on the theory and the practice of the steelyard balance which enjoyed a wide diffusion. Al-ê´fŷ seems to be the last *original* representative of the classical Arabic tradition of works on balances and weights. With him, this tradition arrives at an end, in the same time when pre-classical physics in Europe was operating a deep transformation that will finally integrate the science of weights into modern physics. Here are his main treatises, known in several extant copies preserved exclusively in Cairo and Damascus, attesting to their widespread use in Egypt and Syria over several centuries:

19. *Risêla fŷ ŷinêat al-qabbên* (Treatise in the art of the steelyard): a systematic description of the steelyard and its use in different situations, showing a clear acquaintance with steelyards. The text is explicitly written for the practitioners;

20. *Irshêd al-wazzên li-ma>rifat al-awzên bi 'l-qabbên* (Guide to the weigher in the knowledge of the weights of the steelyard): similar to the previous text;

21. *Risêla fŷ qismat al-qabbên* (Treatise on the division of the steelyard): contains arithmetical and geometrical problems on the calculation of the parts of the steelyard;

22. *Risêla fŷ iŷlêú fasêd al-qabbên* (Treatise on repairing the defectuousity of the steelyard): very detailed analysis of the different cases of deficiency of a steelyard and the solutions to repair these deficiencies.

Other later texts include:

23. *Nukhbat al-zamên fŷ ŷinêat al-qabbên*: a short text on the steelyard by >Uthmên b. >Alêk al-Dŷn al-Dimashqŷ, known as Ibn al-Malik (fl. 1589);

24. *Risêlat al-jawêhir fŷ >ilm al-qabbên* (Treatise of jewels in the science of the steelyard): a ten-chapter text written by *Khiêr al-Burlusŷ al-Qabbênŷ* (d. in 1672).

25. Two writings on the "science" (>ilm) and the "description" (*taŷŷif*) of the steelyard by >Abd al-Majŷd al-Sêem´lŷ (18th century);

26. *Al->lqd al-thamŷn fŷmê yata>allaq bi-'l-mawêzŷn* (The high priced necklace in what concerns the balances), a systematic treatise on the balance and weights, by ê asan al-Jabarŷ (1698-1774);

27. Several short texts dealing with the principles and the construction of the steelyard by Muáammad al-Ghamrŷ (died before 1712);

28. *Risāla fī 'l-qabbān* by Mu'ammad b. al-ī usayn al-ā'ā' (d. 1819), a Syrian author, is among the very last works written in Arabic in the style of the earlier mechanical tradition.²⁶

For some other texts, the authorship is not yet established firmly as they don't bear any name and they are catalogued until now as "anonymous texts". In this last category, we mention the following three tracts, which are very probably connected with the texts of the later period just mentioned above.

29. First, a huge summa titled *Al-qawānīn fī šifat al-qabbān wa 'l-mawāzīn* (The laws in the description of the steelyard and the balances) existing in Codex TR 279, ff. 1-62 in the Cairote Dīr al-kutub.

30. Then a short text, *Bāb fī ma'rifat āmal al-qabbān* (Chapter in the knowledge of making the steelyard) (Cairo, Dīr al-kutub, MS K3831/1 and MS RT 108/1).

31. An untitled tract which the beginning is: "*hādhihi risāla fī āilm al-qabbān*" (Cairo, Dīr al-kutub, in the same codex K3831).

32. And finally two short tracts (*Risāla mukhtašara fī āilm al-qabbān* and *Risāla fī āilm šināat al-qabbān*) preserved in Damascus (National Library, al-ū'hiriyya Collection, MS 4).²⁷

The texts mentioned so far afford a precious testimony to the fact that scientific and technical works – sometimes with a high level of originality– continued to be composed in Arabic in the field of mechanics until the 19th century. This corresponds to similar information derived from recent research in other fields of Arabic sciences, such as astronomy and mathematics. The ongoing research into this later phase of science in the Arabic language will undoubtedly change our appreciation of the historical significance of Arabic science and of its place in the general history of science and culture.

6. The status of the science of weights (*āilm al-athqān*)

The availability of the major part of the Arabic texts on the problems of weights and balances makes it possible, for the first time, to address the question of the historical significance of this large corpus of mechanical works. The investigation of this question has already led to a far-reaching conclusion. It turns out that this corpus represents no less than the transformation of the ancient mechanics into a systematic science of weights and balances. As disclosed in the treatises of Pseudo-Aristotle, Philon, Heron, and Pappus, the Greek classical doctrine of mechanics was shaped as a collection of descriptions and riddles about machines, instruments, and common observation. In contradistinction, the new Arabic science of

²⁶ This treatise is a digest of earlier works composed of an introduction –devoted to the principle of the equilibrium of weights– and 2 chapters on 1. the construction of the steelyard, 2. the conversion of weights between countries. Chap. 1 deals in a didactic way with the elementary properties of the balances and a certain emphasis is made on the law of the lever. The text exists in 3 copies: Damascus, al-Asad Nat. Lib., ū'hir. coll., MS 4297; Aleppo, al-Aūmadiya Lib., al-Maktaba al-waqfiya, MS 1787; Rabat, National Library, MS D 1954.

²⁷ Among these anonymous texts, we should mention a "strange" text preserved in Paris (Bibliothèque Nationale, Fonds Arabe, MS 4946, ff. 79-82) under the title *Nukat al-qarasān* (The secrets or the properties of the steelyard) and ascribed to Thābit ibn Qurra. Its contents are without any doubt related to the science of weights, and its main subject is very elementary and treats of some cases of weighing with the

weights is focused on a relatively small range of subjects – mainly the theory of the balance and equilibrium and the practical issues of weighing with different instruments. On the conceptual level, it is built on a dynamic foundation and seeks to account for mechanical phenomena in terms of motion and force. As such, it restores a strong link between mechanics and natural philosophy. This new science of weight lasted in Arabic culture until the 19th century and constituted since the 12th century a basis for the Latin *scientia de ponderibus* that developed in Western Europe.

The emergence of the Arabic science of weights has been proclaimed by al-Fārābī (ca. 870-950) in his *Uṣūl al-ʿilm*, where he produced an authoritative reflexion on the epistemological status of mechanics that set the stage for the question once and for all. In particular, he set up a demarcation line between the science of weights and the science of machines, and considered both as mathematical disciplines.

Al-Fārābī differentiated in his system between six principal sciences: those of language, logic, mathematics, nature (physics), metaphysics and politics. The mathematics is subdivided into seven disciplines: arithmetics, geometry, perspective, astronomy, music, the science of weights (*>ilm al-athqāl*) and the science of devices or machines (*>ilm al-ūiyyal*). The last two are characterized as follows:

As for the science of weights, it deals with the matters of weights from two standpoints: either by examining weights as much as they are measured or are of use to measure, and this is the investigation of the matters of the doctrine of balances (*<um ʿr al-qawl fī 'l-mawāzīn*), or by examining weights as much as they move or are of use to move, and this is the investigation of the principles of instruments (*<uṣūl al-ʿilāl*) by which heavy things are lifted and carried from one place to another.

As for the science of devices, it is the knowledge of the procedures by which one applies to natural bodies all that was proven to exist in the mathematical sciences... in statements and proofs unto the natural bodies, and [the act of] locating [all that], and establishing it in actuality. The sciences of devices are therefore those that supply the knowledge of the methods and the procedures by which one can contrive to find this applicability and to demonstrate it in actuality in the natural bodies that are perceptible to the senses.²⁸

Considering the two main branches of mechanics as genuine mathematical sciences, al-Fārābī located their objects respectively in the study of weights and machines. Hence, *>ilm al-athqāl* is centered on the principles of the balances and of lifts, investigated with reference to measure and motion, whereas *>ilm al-ūiyyal* is conceived of as the application to natural bodies of mathematical properties (lines, surfaces, volumes, and numbers). As such, it includes various practical crafts: the overseeing of constructions, the measurement of bodies, the making of astronomical, musical, and optical instruments, as well as the fabrication of hydraulic mechanisms, mirrors, and tools like bows, arrows and different weapons.²⁹

steelyard.

²⁸ Al-Fārābī 1949, pp. 88-89.

²⁹ *ʿiyyal* (sing. *ūʿla*) translated the Greek word *mechanē* which means both mechanical instrument and trick and is at the origin of the words machine and mechanics. On the affinities between *mechanē* and *ūʿla*, see Abattouy 2000c.

In this context, the main function of *>ilm al-úyyal* consists in bringing the geometrical properties from potentiality (*quwwa*) to actuality (*fi>l*) and to apply them to real bodies by means of special engines (*bi-'l-šana*).³⁰ Developing an Aristotelian thesis,³¹ al-Fārābī endows the science of machines with an eminent task, to actualise the mathematical properties in natural bodies. Such a function of actualisation could not be extended to *>ilm al-athqāl*. In fact, weight and motion, the two notions that delimit its field of investigation, can hardly be taken as geometric properties of natural bodies, limited by al-Fārābī to spatial and numerical aspects, in accordance with the canonical Euclidean paradigm that banishes all the material properties of magnitudes from the realm of geometry.

The distinction of the science of weights from the different crafts of practical mechanics is a crucial result of al-Fārābī's theory. The emphasis laid by the Second Master on *>ilm al-athqāl* can not be stressed enough. It means no less than a solemn announcement of the emergence of an independent science of weights. With roots in the long tradition of the ancient mechanics, this new discipline came to light in the second half of the 9th century in the works of Thābit ibn Qurra and his colleagues.³² It is this important scientific achievement that was recorded by al-Fārābī while building his system of knowledge.

Al-Fārābī's thesis had a long-lasting resonance in Arabic learning and was never challenged seriously. The fundamental singularity of the science of weights as an independent branch under the mathematical arts, distinct from the science of machines, became a feature of subsequent theories of science. For confirmation a great number of instances, in different kinds of works and in various literary contexts, can be called upon. Hereinafter, some of these instances are presented in chronological order.

In his *Risāla fī aqsām al-ʿulūm al-ʿaqliyya* (Epistle on the parts of rational sciences), Ibn Sīnā (980-1037) enumerated the mechanical arts, considered as 'secondary constituents' of geometry, as *>ilm al-úyyal al-mutaʿarrika* (the science of movable machines, i.e., automata),³³ the pulling of weights (*jarr al-athqāl*), the science of weights and balances (*>ilm al-awzān wa al-mawāzīn*), and the 'science of particular machines' (*>ilm al-ʿilāl al-juzʿiyya*).³⁴ Ibn Sīnā establishes a clear distinction between the science of weights and balances, the craft of pulling heavy loads, and the art of devices. In addition, the latter is subdivided into the arts of automata and of particular machines. Likewise, the pulling of weights, included in the science of weights by al-Fārābī, is assigned as a specific branch of geometry. The main point, however, in Ibn Sīnā's schema is the emphasis laid on the science of *awzān* and *mawāzīn* in which weights and balances are combined. The reference to the *wāzn* instead of the *thiqāl* could be interpreted as a privilege given to the statical standpoint. Indeed, the *wāzn* is a constant quantity measurable in a

³⁰ In the Arabic partial version of Pseudo-Aristotle's *Mechanical Problems*, this very function of the *úyyal* is said to be carried out with artificial devices (*úyyal šinʿiyya*): see the edition of the *Nuṭaf min al-úyyal* in Abattouy 2001a, pp. 110, 113 and Aristotle 1952, 847a 25-30. The function of *>ilm al-úyyal* as actualisation of potentialities is surveyed in Saliba 1985.

³¹ Aristotle, *Metaphysics* XIII.3, 1078 a 14-16.

³² The thesis of the birth of the Arabic science of weights was first formulated in Abattouy, Renn and Weing 2001.

³³ That *al-ʿilāl al-mutaʿarrika* refers to automata is established in Abattouy 2000c, pp. 139-140.

³⁴ The other components of geometry are the sciences of measurement, of optics and mirrors, and of hydraulics: see Anawati 1977, p. 330 and Ibn Sīnā 1989, p. 112.

balance, whereas the *thiq* is that quantity –called gravity or heaviness– which varies during the weighing process and depends on the position of the weighed object relatively to a particular point, the center of the world or the fulcrum of the balance.³⁵

In his discussion on the divisions of sciences in *Maqāṣid al-falāsifa* (The Intentions of philosophers), al-Ghazālī (1058-1111) subsumed the science of weights (*>ilm al-athqāl*) as an independent branch under the mathematical arts and differentiates it from the study of ingenious devices (*>ilm al-úyya*).³⁶ Ibn Rashīq, a Moroccan mathematician of the late 13th century from Sebta, assumed a similar demarcation between weights and machines, and founded the latter on the former: the science of weights, of balances, and of catapults (*>ilm al-athqāl wa 'l-mawāzīn wa 'l-majānīq*) deals with the downward motion of heavy bodies and constitutes the foundation of the science of machines (*wa-yatarattab >alē >ilm al-athqāl >ilm al-úyya*).³⁷ In his biography of al-Isfizerī, al-Bayhaqī did not confuse the two when he reported that al-Isfizerī “was mostly inclined to astronomy and to the science of weights and machines (*>ilm al-athqāl wa al-úyya*).”³⁸ This corresponds to what we know of his extant works in mechanics, the *Irshād* being clearly a book of *athqāl*, whereas al-Isfizerī’s work on *úyya* is represented by a collection of compiled summaries (sometimes with comments) extracted from the mechanical works of Heron, Apollonius and Ban ‘ M ‘sī.³⁹ Later on, Taqī al-Dīn ibn Maṣrūf, the 16th-century mechanician, followed the same pattern. Accounting for the books he read in his scientific curriculum, he mentioned, in addition to texts of mathematics, “books of accurate machines (*kutub al-úyya al-daqqā*), treatises of the science of the steelyard and of the balance (*rasā'il >ilm al-qarasān wa al-māzān*), and of the pulling of weights (*jar al-athqāl*).”⁴⁰

Sometimes *>ilm al-athqāl* is referred to as *>ilm marḥkiz al-athqāl*, one of its branches which enjoyed great reputation. A good instance of this is the following quotation we find in the correspondence between al-Q ‘hī and al-ġabbī. In a letter to al-Q ‘hī, al-ġabbī says:

³⁵ The difference is well illustrated by the definition opening Pseudo-Euclid’s *Maqāla fī 'l-māzān*: “weight (*wazn*) is the measure of heaviness (*thiq*) and lightness (*khiffa*) of one thing compared to another by means of a balance”: Paris, Bibliothèque Nationale, MS 2457, f. 22b.

³⁶ Al-Ghazālī 1961, p. 139.

³⁷ Al-ī usayn b. Abī Bakr Ibn Rashīq (d. 1292), *Risālat fī taṣnīf al-ūl ‘m al-riyāḥiyya*, Rabat, al-Maktaba al-‘mma, MS Q 416, p. 422. On Ibn Rashīq, see Lamrabet 2002 and Abattouy 2003a, pp. 101-105.

³⁸ Al-Bayhaqī 1988, p. 125. Likewise, in the notice he devoted to the mathematician Ab ‘ Sahl al-Q ‘hī, al-Bayhaqī states that he was “well-versed in the science[s?] of machines and weights and moving spheres” (*baraza fī >ilm al-úyya wa al-athqāl wa al-ukar al-mutawārrika*) (ibid., p. 88).

³⁹ In the incipit of this collection, al-Isfizerī writes: “We collected in this book what has reached us of the books on various devices (*anwā' al-úyya*) composed by the ancients and by those who came after them, like the book of Philon the constructor of machines (*sūb al-úyya*), the book of Heron the mechanician (*ḥrun al-majānīq*) on the machines (*úyya*) by which heavy loads are lifted by a small force... We start by presenting the drawings of the machines (*ṣūwar al-úyya*) conceived by the brothers Mu‘ammad, A‘amad and al-ī asan, Ban ‘ M ‘sī ibn Shīkir.” Manchester, John Ryland Library, Codex 351, f. 94b; Hayderabad, Andra Pradesh Library, Asāfiyya Collection, Codex QO 620, p. 1.

⁴⁰ In his *Kitāb al-uruq al-saniyya fī al-‘līet al-r ‘ūniyya* (The Sublim methods in spiritual machines): al-ī asan 1976, p. 24.

*We did not obtain a complete book on this science, I mean centers of gravity (marʿikiz al-athqal), nor was there done any satisfactory work by one of the ancients or one of the moderns. In my opinion it is in the rank of a singular science which merits to have a book of basic principles (al-ṣinʿa al-mufrada allatī yuʿtīj an yuḥmal lahā kitāb uṣūl).*⁴¹

A century later, al-Isfizārī qualified the centers of gravity as “the most elevated and honourable of the parts of the mathematical sciences” and defined it as:

*the knowledge of the weights of loads of different quantities by the [determination of the] difference of their distances from their counterweights.*⁴²

Al-Khazīnī specifies further the definition of his predecessor when he explains that the study of the steelyard is founded upon the science of the centers of gravity (*wa ʾalayhi mabnʿ al-qaffʿin*).⁴³ Therefore, it is obvious that the expression *marʿikiz al-athqal* is intended to account for the static aspect of *ʾilm al-athqal*, by the study of forces as they are related to weights, such as in the case of levers and scales. This same thesis is assumed by other Islamic scholars.⁴⁴

In contrast, the tradition of *ʿiyyal* delimits the contours of a distinct discipline, centered on the investigation of the methods of applicability of mathematical knowledge to natural bodies. As represented in several Greek and Arabic mechanical texts, written by Heron, Pappus, Philon, Ban ʿ Māsʿ and al-Jazarī, the tradition of *ʿiyyal* is focused on the description of machines and the explanation of their functions. Book I of Heron’s treatise contains principles of theoretical mechanics, but the rest, more than three quarters of the whole, is predominantly about different kinds of devices. The same applies to the treatise of Pappus. As for Philon of Byzantium (fl. 230), his *Pneumatics* is mainly a catalogue of machines worked by air pressure.⁴⁵

An important constituent of the Greek traditional doctrine of mechanics –as it is disclosed in the texts by Pseudo-Aristotle, Heron and Pappus– is represented by the theory of the simple machines (the windlass, the lever, the pulley, the wedge, and the screw). Those simple machines were dealt with in Arabic science by several scholars such as the Pseudo-Ibn Sīnā,⁴⁶ al-Isfizārī,⁴⁷ and Sinʿan ibn Thʿabit⁴⁸ under the name

⁴¹ Berggren 1983, pp. 48, 120.

⁴² *Irshād dhawʿ al-ʾirfān ilā ṣinʿat al-qaffʿin*, al-ʿAsad National Library in Damascus, al-ʿUthiriyya collection, MS 4460, f. 16b.

⁴³ Al-Khazīnī 1940, p. 5.

⁴⁴ For instance, Ibn al-Akfānī (fourteenth century) asserts that *ʾilm marʿikiz al-athqal* shows “how to balance great weights by small ones, with the intermediary of the distance, such as in the steelyard (*qaras: ʿn*)”: Ibn al-Akfānī 1989, p. 409. The same idea is in al-Tahānawī 1980, vol. 1, p. 47.

⁴⁵ Philon’s *Pneumatics* was translated into Arabic under the title *Kitāb Fī ʿn fī al-ʿiyyal al-rʿūʿniyya wa mʿjanq al-mʿ* (The Book of Philon on spiritual machines and the hydraulic machines). The Arabic text was edited and translated into French in Carra de Vaux: see Philon 1902.

⁴⁶ A Persian mechanical text called *Miʾyār al-ʾuq ʿl dur fan jar athqal* is attributed to Ibn Sīnā. The treatise, in two sections, is devoted to the five simple machines. It presents the first successful and complete attempt to classify simple machines and their combinations: Ibn Sīnā 1331 H [1952]. For a short commentary, see Rozhanskaya 1996, pp. 633-34.

⁴⁷ Al-Isfizārī is the author of a collection of summaries and commentaries extracted from the mechanical works of Heron, Apollonius, and

of *úiyyal*. Besides this trend on the basic simple machines and their combinations, the science of *úiyyal* also included a description of other categories of machines necessary in daily life and useful for civil engineering. The most well known works describing this kind of engines are the texts of machines by Ban´ M´ sĒ and al-Jazarġ. *KitĒb al-úiyyal* by the Ban´ M´ sĒ comprises a large variety of devices, the vast majority of which consist of trick vessels for dispensing liquids. The book of al-Jazarġ *al-JĒmi> bayna 'l->ilm wa 'l->amal fġ ŒinĒ>at al-úiyyal* (*The Compendium of theory and practice in the art of mechanics*) enlarges this same feature in an unprecedented way. The author incorporates in it the results of 25 years of research and practice on various mechanical devices (automata, musical machines, clocks, fountains, vessels, water-raising machines, etc.)⁴⁹

The conception of *úiyyal* as the practical component of mechanics is additionally corroborated by the contents of a chapter of the *MafĒtġū al->ul´m* by Muúammad b. Y´ suf al-KhwĒrizmġ (10th century). Chapter 8 of Book II of this lexicographic encyclopedia is dedicated to "*ŒinĒ>at al-úiyyal, tusammĒ bi al-y´nĒniyya manjanġq´n*" (the art of mechanics, called in Greek *manjanġq´n*). Besides a short mention of machines for the traction of weights, the *úiyyal* described are essentially of two types: automata (*ĒĒĒt al-úarakĒt*) and hydraulic devices (*úiyyal úarakĒt al-mĒ>*).⁵⁰ The author devotes great attention to the first two kinds; this might be taken as evidence to the preeminence of these machines in the domain of *úiyyal* in his time. Significantly, al-KhwĒrizmġ – like Ibn SġnĒ – classifies the weight-pulling machines in the field of *úiyyal* in contrast to their arrangement among that of *athqĒl* by al-FĒĒĒbġ, which should be considered as an evolution in the sense of narrowing and précising the domain of weights, thus articulated around the ideal model of the study of balances and measures.

The analysis of the overall significance of the Arabic medieval science of weights showed that this tradition does not represent a mere continuation of the traditional doctrine of mechanics as inherited from the Greeks. Rather, it means the emergence of a new science of weights recognized very early on in Arabic learning as a specific branch of mechanics, and embodied in a large scientific and technical corpus. Comprehensive attempts at collecting and systematizing (as well as updating with original contributions) the mainly fragmentary and unorganized Greco-Roman mechanical literature that had been translated into Arabic were highly successful in producing a coherent and orderly mechanical system. In this light, a redefinition of Arabic mechanics becomes necessary, initially by questioning its status as a unified field of knowledge. Such a redefinition may be worked out briefly by setting a sharp distinction between *>ilm al-athqĒl* and *>ilm al-úiyyal*. The latter corresponds to the traditional descriptive doctrine of machines, whereas the core structure of the *>ilm al-athqĒl* is a genuine theory of mechanics articulated around the balance-lever model and its theoretical and practical elaborations. Uniting the theoretical treatment of the balance with concrete practical information about its construction and use, and adopting an integrative

Ban´ M´ sĒ. He dealt with simple machines in his commentary on Book II of Heron's *Mechanics*: see Abattouy 2000b, pp. 147-48.

⁴⁸ SinĒn (d. 942), the son of ThĒbit ibn Qurra, is presumably the author of a fragment on the five simple machines preserved in Berlin, Staatsbibliothek, MS Orient fol. 3306.

⁴⁹ For the two works of Ban´ M´ sĒ and al-Jazarġ, see respectively Hill 1974 and Hill 1979 for English translations and al-Ē asan 1979 and al-Ē asan 1981 for the Arabic texts.

⁵⁰ Al-KhwĒrizmġ 1968, pp. 246-247.

treatment of physics and mechanics, overcoming their original separation in Antiquity, the new science of weights distinguishes itself by turning mechanics from being originally a marginal part of geometry into an independent science of weights.

On the methodological level, the new science of weights was marked by a close combination of experimentation with mathematisation. The Aristotelian qualitative procedures were enriched with quantitative ones, and mathematics was massively introduced in the study of mechanical problems. As a result, mechanics became more quantitative and the results of measures and experiments took more and more weight in mechanical knowledge. Certainly, the fundamental concepts of Aristotelian physics continued to lay in the background, but the scholars were able to cross their boundaries and to accomplish remarkable discoveries in physical ideas. For instance, the generalization of the theory of centers of gravity to three-dimensional objects, the introduction of a dynamic approach in the study of problems of statics and hydrostatics, the improvement of the procedures and methods for the determination of specific weights and of weighing instruments, the development of the theory of heaviness and the establishment of a theory of the ponderable lever. Further, the treatment of the law of equilibrium by Thĕbit ibn Qurra and al-Isfizĕrĳ opened the horizon of a unified theory of motion in which the dichotomies of natural-violent, upward-downward motions vanish, exactly as they disappear in the concomitant motions of the two arms of a balance lever. In this physical system, indeed, the weight of the body might be considered the cause of the downward as well as of the upward motion, overcoming the Aristotelian balking at making weight a cause of motion. For their parts, al-Q ħĳ and Ibn al-Haytham had the priority in formulating the hypothesis that the heaviness of bodies vary with their distance from a specific point, the center of the earth. Moreover, they contributed to unify the two notions of heaviness, with respect to the center of the universe and with respect to the axis of suspension of a lever. In his recession of the works of his predecessors, al-Khĕzinĳ pushed forward this idea and drew from it a spectacular consequence regarding the variation of gravity with the distance from the centre of the world. All this work represented strong antecedents to the concept of positional weight (*gravitas secundum situm*) formulated by Jordanus in the 13th century.⁵¹

The historians of mechanics, from Pierre Duhem until Marshal Clagett, assumed that the foundation of the science of weights must be credited to the school of Jordanus in Europe in the 13th century. Now it appears that this science emerged much earlier in Islamic science, in the 9th century. Moreover, the first steps of the Latin *scientia de ponderibus* should be considered as a direct result of the Arabic-Latin transmission, and especially as a consequence of the translation of two major Arabic texts in which the new science and its name are disclosed, *Kitĕb fĳ 'l-qarasĳ n* by Thĕbit ibn Qurra and *Iűűĕ al-űul ĳm* by al-Fĕrĕbĳ.

Indeed, the very expression *scientia de ponderibus* was derived from the Latin translation of al-Fĕrĕbĳ's *Iűűĕ al-űul ĳm*. Versions of this text were produced both by Gerard of Cremona and Dominicus Gundissalinus. The latter made an adapted version of the *Iűűĕ* in his *De scientiis* and used it as a framework for his own *De divisione philosophiae*, which later became a guide to the relationships between the sciences for European universities in the 13th century. In the two texts, Gundissalinus reproduced –

⁵¹ It is evident that all these issues need to be treated and instantiated separately and thoroughly, as they document the theoretical components of the new science of weight: see for a first analysis Abattouy 2001b and Abattouy 2002a. The interpretation of the Arabic science of weights as a progress of science is developed in Abattouy 2004a.

sometimes verbatim— al-Fārābī's characterization of the sciences of weights and devices, called respectively *scientia de ponderibus* and *scientia de ingeniis*.⁵² The reason for this close agreement is easy to find: he could not rely on any scientific activity in this field in his times in Latin.⁵³ Among all the sciences to which Gundissalinus dedicated a section, the sciences of weights, of devices, and of optics were obviously less known in the Latin west in the 12th century. Even the antique Latin tradition represented by Boece and Isidore of Sevilla could not furnish any useful data for a sustained reflexion on their epistemological status. It must be added also that Gundissalinus seems to ignore all their developments in the Arabic science either, including Thābit ibn Qurra's book on the theory of the balance and Ibn al-Haytham's achievements in optics. Hence, the effort of theorization deployed by Gundissalinus, by showing the state of the sciences in the late 12th century in Western Europe, throws the light on a considerable underdevelopment in several sciences. This concerns particularly the different branches of mechanics.⁵⁴

As said before, *Liber karastonis* is the Latin translation by Gerard of Cremona of *Kitāb fī 'l-qaras^h n*. The general structure is the same in both Arabic and Latin versions, and the enunciations of the theorems are identical. Yet the proofs might show greater or lesser discrepancies. None of the Arabic extant copies of Thābit's *Kitāb* seem to be the direct model for Gerard's translation. The Latin version was repeatedly copied and distributed in the Latin West until the 17th century, as it is documented by several dozens of extant manuscript copies. This high number of copies instructs on the wide diffusion of the text. Further, the treatise was embedded into the corpus of the science of weights which was understood to be part of the mathematical arts or quadrivium, together with other works on the same topic, in particular the writings of Jordanus Nemorarius in the science of weights.⁵⁵ In addition, at least one version of Thābit's work was known in Latin learning as a writing of *scientia de ponderibus*. This version is the *Excerptum de libro Thebit de ponderibus*, a Latin text which appears frequently in the codexes. It is precisely a digest of the logical structure of *Liber de karastonis*, in the shape of statements of all the theorems.⁵⁶

7. Mechanics in the service of society

This final section will be dedicated to a preliminary overview on the institutional setting of the usage of the balance in medieval Islamic societies. The focus will be laid on a brief description of the role the *ūisba* office played in the control of the fabrication and usage of weighing instruments

The balance most widely used in the Islamic lands of medieval times was the equal-armed platform scale, made mostly in copper. There were tiny balances for gold and jewels, average ones for retail traders, and

⁵² Gundissalinus 1903, *De Div. Phil.*, pp. 121-24 and Gundissalinus 1932, *De Scientiis*, pp. 108-112.

⁵³ It is to be noted that Hughes de Saint Victor who, in his *Didascalicon de studio legendi*, provided the most complete Latin classification of the sciences before the introduction of Arabic learning, just overlooked the two mechanical arts. On the *Didascalicon* see Taylor 1991.

⁵⁴ This was noted by Hugonnard-Roche 1984, p. 48. Other Arabic works on the classification of the sciences translated into Latin might have been a source for the distinction of the science of weights and its qualification as the theoretical basis of mechanics. For instance, al-Ghazālī's *Maqāṣid al-falāsifa*, translated as *Summa theoricæ philosophiæ* by Gundissalinus and Johannes Hispanus in Toledo, and Ibn Sīnā's *Risāla fī aqsām al-^hm*, translated by Andrea Alpago: *In Avicennæ philosophi præclarissimi ac medicorum principis, Compendium de anima, De mahad..., Aphorismi de anima, De diffinitionibus et quæstis, De divisione scientiarum*, Venice, 1546, fols 139v-145v.

⁵⁵ The *Liber karastonis* is edited with English translation in Moody and Clagett 1952, pp. 88-117. For more details on its codicological tradition, see Buchner 1922 and Brown 1967.

⁵⁶ Brown, 1967, pp. 24-30 and Knorr, 1982, pp. 42-46, 173-80.

huge balances for the merchants of grains, wood, wool, etc. In general, the balances had beams and weights made of steel or iron. Steelyards, called *qaras^ʿn* or *qabb^lEn*, were also widely employed. As reported in a historical source,⁵⁷ a site called *Qaras^ʿn* existed in the ancient medina in Fez until the early 20th century, probably because of a huge public balance set up there. Public balances are still located today in the *fan^lEdiq* (bazaars) of the old medina. One can infer in this context that a similar public weighing site must have been present in all the markets of Islamic cities.

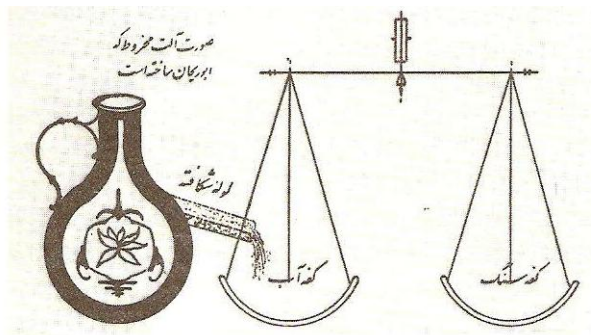


Figure 3. Al-Birūni's balance, in Seyyed Hossein Nasr. *Islamic Science an Illustrated Study*. Kent 1976 (The image was introduced by the editor).

The *qaras^ʿn* or steelyard with a sliding weight was largely used since Antiquity. It is mentioned in Greek sources by its ancient name, the *chariston*, and was employed extensively in Roman times.⁵⁸ Composed of a lever or a beam (*am^ʿd*) suspended by a handle that divides it into two unequal arms, the center of gravity of the instrument is located under the fulcrum. In general the shorter arm bears a basin or a scale-pan in which the object to be weighed is set, or suspended from a hook. The cursor-weight, *rumm^lEna* in Arabic, moves along the longer arm in order to achieve equilibrium. This arm, which has generally a quadrangular cross section, bears two different scales which are engraved along the two opposite sides. Due to the fact that the steelyard can be suspended by two hooks, there are two independent graduations. According to the choice made, there will be different relations between the lengths of the longer and smaller arms of the lever, corresponding to the different scales. On the beam or near the fulcrum, the number of units or fractions corresponding to the capacity of the balance was engraved as was the official stamp of the authorities. The advantage of the steelyard is that it provides an acceptable precision in weighing and allows heavy loads to be supported by small counterweights. In addition, it can be carried around easily.

Another kind of balance is a combination of the ordinary balance and of the steelyard in the form of an equal-armed balance with mobile weight. A typical example of this instrument is the balance of Archimedes described by al-Kh^lEzin^ʿ according to an account by Menelaus.⁵⁹ In addition to its two equal arms to which two fixed scale pans are suspended, this balance had on one of the arms a cursor weight which could be hang up on different points of a small scale graduated in two series of divisions. Presented as an

⁵⁷ Dozy 1927, vol. 2, p. 327.

⁵⁸ On the ancient history of the steelyard, see Ibel 1908 and Damerow et al. 2002.

hydrostatical balance for the determination of specific gravities, it could also serve for ordinary weighing. A variety of the Archimedes' balance consists in moving the scale pan on a part of the arm. This is the main property of the *māzān al-ḥaqīq* (natural or physical balance) designed by Muḥammad ibn Zakariyyā al-Rāzī. In this model with equal arms and without counterpoise, one of the scale pans is movable and might behave as a counterweight.

Nowadays, the steelyard balance is called in some Arab countries *al-māzān al-qabbānī*; in Morocco it is designated as *māzān al-qura*. Despite the introduction of modern balances more or less sophisticated, since long time ago (in the first half of the 19th century), the steelyards continue to be utilized in Arab and Islamic countries. They serve in popular markets and are widely used in some activities, such as in the slaughterhouses and in the shops of butchers. In Egypt, the industry of traditional steelyards is still active. Egyptian colleagues informed me that in the old city of Cairo, in an area called *al-ayyūn al-rubāʿī*, near the *al-kutub*, not far from the Azhar Mosque, artisans build steelyards according to traditional methods. These balances are used massively throughout the country, for example in the weighing of cotton in the country side. In other Arab countries, the fabrication of these balance disappeared completely. For instance, in Morocco, it vanished since several decades, as a result of the introduction of modern balances and of the concurrence of the European industry of these same instruments. Therefore, the steelyards used in the country are imported from Southern Italy and Spain. But local artisans are able to repair the imported engines and to supply certain of their equipments, as I could see by direct observation during my visits to their shops in Fez in 1999 and 2000.

In his geographical book *Aḥsān al-taqḍīm fī maʿrifat al-aqḍīm*, Muḥammad al-Muqaddasī, the Palestinian geographer of the 10th century, reports that the most accurate balances were those fabricated at *al-ʿIrāq* in northern Mesopotamia. *Kāfā*, in southern Iraq, was also famous for the accuracy of its balances. Other regions were celebrated for the honesty of the weighing practices of their merchants, such as *al-Kharrāb*. But others were better known for their fraudulent procedures. Various passages in the *Qurʾān* show that as early as the advent of Islam, false balances were in use in the markets. Later narratives report that some jewelers and goldsmiths, in order to fraudulently weigh their wares, blow gently on the scale-pan of their balance, stick a small piece of wax under it, or merely use false weights. Al-Jawbarī (fl. 1216-22) described two such arrangements. In the one the beam of the balance consisted of a hollow reed containing quicksilver, which was closed at both ends. By a slight inclination of the beam, the quicksilver could be made to flow as desired to the side with weights or with goods and thus make one or the other appear heavier. In the other case, the tongue of the balance was of iron and the merchant had a ring with a magnetic stone; by bringing the ring close to the balance, it moves down to the right or left.⁶⁰

In order to reprimand these fraudulent tricks and deceitful behaviour, and to implement the instructions of Islam about the strict observance of the just weighing, the Islamic society invented a specific institutional setting, represented by the office of *al-ʿisba*. This office was occupied by the *muʿtasib*, an officer regularly appointed to take charge of the harmonization between the commands of Islam and the social practice,

⁵⁹ Al-Kharrābī 1940, pp. 78-79.

⁶⁰ Al-Jawbarī 1979-80, vol. 2, p. 162. Similar fraudulent practices are described in detail in the books of *al-ʿisba*: for references to the *al-ʿisba* literature relevant to the balances and weights knowledge, see Abattouy [Forthcoming 2006].

especially concerning the control of markets. As such, one of his main duties was to observe that correct scales and weights were used in commercial transactions.

The office of *úisba* was established towards the 2nd century of Hijra as a consequence of the development of large cities and after that the various schools of *fiqh* (jurisprudence) assumed form. With the establishment of the new office, certain text-books began to include chapters dealing with the theory of its functions and their practical application, and in the course of time independent manuals intended to assist the *muútasib* in the performance of his duties were written. Among these text-books, the best known are *NihÉyat al-rutba fÉ alab al-úisba* by Abd-al-Rahman al-ShayzarÉ (d. 589/1193), and *MaÉElim al-qurbÉ fÉ aukÉm al-úisba*, by ÉiyyÉ al-DÉn al-QurashÉ, known as Ibn al-Ukhuwwa (d. 729/1329). The manuals for the guidance of the *muútasib* are an important source for the reconstruction of the social structures within which the making and the use of the balances and weights were organized and regulated in medieval Islam.

The *muútasib* was in charge of the morality, integrity, and quality of the various trades, but his main duty, the basic and permanent one, was to watch over and to supervise the balances and weights. In his *NihÉyat al-rutba fÉ alab al-úisba* (The utmost authority in the pursuit of *úisba*), the earliest extant book of its kind to appear in the Islamic East, al-ShayzarÉ defines as follows the duties of the *muútasib* in this domain:

The most accurate scale is that in which the two sides are equal, the pans are balanced and the hole for the attachment on either side of the centre of the beam is one third of the thickness of the attachment. The hole should be one third of the way under the peg of the attachment, and two thirds above it. This allows for the inclination of the scales by taking the tongue of the balance out of the beam of the attachment, and the pan will descend with the slightest weight (...). The peg might be square, triangular or round. The best is the triangular one because it inclines with more sensitivity than the others.

The muútasib must order those who use scales to wipe and clean them hourly of any oil or dirt, as a drop of oil may congeal on them and affect the weights. The merchant must settle the scales before he begins to weigh and should place the merchandise on them gently, not dropping it into the pan from his raised hand, nor moving the edge of the pan with his thumb, as all of this is fraudulent...

The merchant should acquire raÉl-s and awqiyya-s made of iron and test their accuracy against the standard weights. He must not use stone ones, as this chip when they knock against each other and thus become inaccurate. If stone weights have to be used because iron ones are unavailable, then the muútasib must order the merchant to bind them with leather and he must stamp them

after testing their accuracy. He should re-examine them now and again in case the merchant has replaced them with wooden weights which look the same.⁶¹

In the 13th-century Fatimid Cairo, the fabrication as well as the control of the balances and weights was undertaken within a specific institution, the *DĒr al-iyġĒr*, itself under the supervision of the *muútasib*. In his *al-MawĒil wa 'l-*i>tibĒr fġ dhikr el-khi<a< wal-ĒthĒr**, al-Maqrġzġ (1364-1442) provides a valuable report about this institution and shows in a new light the duties of the *muútasib* in the regulation of balances and weights:

The muútasib inspects the DĒr al-iyġĒr... The standard measures were in a place known as the DĒr al-iyġĒr in which the accuracy of all the parts of scales and all the weights were checked. He used to pay the costs of this DĒr, and whatever was needed of copper, steel, wood, glass and other apparatus, and the wages of the workmen, overseers and such like, from the government administration. The muútasib and his deputies would go there to check in his presence the accuracy of what was produced in it. If it was correct, he endorsed it, and if not then he ordered that it should be re-made until it was correct. In this DĒr were specimens with which he corrected the standard measure; for the weights, scales and measures would not be sold except from this DĒr. All the merchants would go to this DĒr upon the muútasib's summoning them, bringing their scales, weights and measures to be tested every so often. If a deficiency was found then the [scale, etc.] was destroyed and its owner was taken to the DĒr and compelled to purchase a replacement from that which was accurately manufactured there, and to pay its price. Then he is forgiven. (...) This DĒr still remains in all of the Fatimid states. When SalĒú al-Dġn took over the government he confirmed this DĒr ... and it still remains.⁶²

According to this report, the *DĒr al-iyġĒr* was in fact the factory where legal balances and weights were fabricated and tested under the control of the *muútasib* and his collaborators. It also comprised the office in which the standard weights were kept. The merchants had to test their usual weights against these legal weights. In the light of this report, it becomes clear therefore why the authors of the Ayyubid, Mameluk and Ottoman Egypt and Syria were so prolific in the composition of technical treatises on the construction of balances, especially of the steelyard type, and on their reparation and testing. There was a strong social demand on them.

The *DĒr al-iyġĒr*, the *úisba* office and similar other institutions provided the Islamic society with the institutional setting for the control of the balances, weights, and measures. These institutions must have been connected in one way or another to the scientific and technical activities shaped of the scientists involved in what we called the science of weights. Indeed, the scientific discoveries and the technical improvements must have provided the controllers of scales and weights with the knowledge and expertise to accomplish their task. In fact, it is easy to demonstrate that the large amount of texts on different sorts

⁶¹ Al-Shayzarġ 1999, pp. 43-44. The same instructions are in Ibn al-Ukhuwwa 1938, pp. 80 ff. and in other manuals of *úisba*: see ZiyġĒda 1962 and Izzi Dien 1997.

⁶² Quoted in Buckley 1992, p. 86.

of balance written in Arabic between the 9th and the 19th centuries were not intended to remain solely in the circle of scientists. At least a substantial part of them was surely addressed to practitioners and artisans, and to the state officials overseeing the markets. This is another instance of the connection between science and society in medieval Islam which deserves a closer investigation.⁶³

References

1. Abattouy, Mohammed 1999. "The Arabic Tradition of Mechanics: Textual and Historical Characterization." *Majallat kulliyat al-ʿAdab wa 'l-ʿulm al-Insaniyya bi-Fes*, vol. 12.1 (1999): pp. 75-109.
2. 2000a. "La Tradition arabe de la balance: Thabit ibn Qurra et al-Khazin." In *Quelques aspects de l'évolution des idées scientifiques. Antiquité et moyen âge*. Rabat: The Faculty of Letters Press, pp. 49-91.
3. 2000b. "Al-Muḥaffar al-Isfiziri ʿElim min al-qarnayn 5-6 H/11-12, mu-allif *Irshad dhawʿ al-irfan ila šinʿat al-qaffiri*". In *Ibid (Quelques aspects de l'évolution des idées scientifiques)*, pp. 135-175.
4. 2000c. "Mechané vs. úiyal: Essai d'analyse sémantique et conceptuelle." In *Imagination and Science*. Rabat: The Faculty of Letters Press, pp. 127-151.
5. 2000d. "Sur quelques démonstrations grecques et arabes de la loi du levier: transmission et transformation." In *Iyyat al-istidlal fi 'l-ilm*. Rabat: The Faculty of Letters Press, pp. 7-43
6. 2001a. "Nutaf min al-úiyal: A Partial Arabic version of Pseudo-Aristotle's *Mechanica Problemata*." *Early Science and Medicine* (Leiden) vol. 6: pp. 96-122.
7. 2001b. "Greek Mechanics in Arabic Context: Thabit ibn Qurra, al-Isfiziri and the Arabic Traditions of Aristotelian and Euclidean Mechanics." *Science in Context* (Cambridge University Press) vol. 14: pp. 179-247.
8. 2002a. "The Aristotelian Foundations of Arabic Mechanics (Ninth-Twelfth centuries)." In *The Dynamics of Aristotelian Natural Philosophy from Antiquity to the Seventeenth Century*. Edited by C. Lüthy, C. Leijenhorst and H. Thijssen. Leiden: Brill, pp. 109-140.
9. 2002b. "The Arabic Science of weights: A Report on an Ongoing Research Project." *BRIIFS. The Bulletin of the Royal Institute for Inter-Faith Studies* (Amman) vol. 4: pp. 109-130.
10. 2003a. "ʿUlīm al-makānik fi al-gharb al-islāmī al-waṣṣ: dirʿasa awwaliyya" (The mechanical sciences in the medieval Islamic west: a preliminary study). In *La Pensée Scientifique au Maghreb: le Haut Moyen Age*. Rabat: The Faculty of Letters Press, pp. 91-121.
11. 2004a. "Min ʿilm al-úiyāl ila ʿilm al-athqāl: wilʿada thaniyya li-l-makānik" (From the science of machines to the science of weights: a new birth of mechanics). In *Mafhīm al-taqaddum fi 'l-ilm* (The concept of progress in science). Rabat: The Faculty of Letters Press, pp. 89-109.
12. 2004b. "Science des poids et úisba: Prolégomènes à l'étude des structures sociales de la mécanique arabe médiévale." In *Les éléments paradigmatiques, thématiques et stylistiques dans la pensée scientifique*. Rabat: Publications de la Faculté des Lettres, pp. 119-130.
13. 2004c. "Išīʿū comme un mode éditorial d'appropriation: la tradition arabe de *Maqāla fi 'l-mẓen* un traité sur la théorie du levier attribué à Euclide." *Majallat kulliyat al-ʿAdab wa 'l-ʿulm al-Insaniyya bi-Fes* (Fes), N° 13: pp. 153-193.

⁶³ A preliminary study of the interaction of the *úisba* institution with the science of weights may be found in Abattouy 2004b. A partial survey of the doctrinal basis of the institution of *úisba*, mainly in the Islamic west, is in Abattouy 2005a.

14. Abattouy 2004-2005. Entries "al-Ahwāzī", "Ilyā al-Maḥrīn", "al-Isfīzī", "Taqī al-Dīn ibn Maḥrīf" (in Arabic). In *Mawsūʿat al-ʿulam al-ʿulam wa 'l-ʿudabāʿ al-muslimīn* (8 volumes to date). Published by the Arab League Educational, Cultural and Scientific Organization (Tunis) and Dar al-Jayl (Beirut).
15. 2005a. "Al-ʿasās al-kalāmī li-muʿassasat al-ʿūsba fī al-gharb al-islāmī" (The *kalāmī* foundation of the institution of *hisbā*). In *Al-ittijāhāt al-kalāmīya fī al-gharb al-islāmī* (The trends of *kalām* in the Islamic west). Rabat: The Faculty of Letters Press, pp. 293-308.
16. 2005b. "Al-Qisṣ al-Mustaqīm: la balance droite de Omar Khayyām." *Farhang. Quarterly Journal of Humanities and Cultural Studies* (Tehran). Issue Topic: *Commemoration of Khayyām* (3), vol. 18, n.53-54, pp.155-166.
17. [In Press 2006a]. *Etudes d'Histoire des Sciences Arabes*. Edited by Mohammed Abattouy. Casablanca: Publications of the King Abdulaziz Foundation for the Humanities and the Islamic Studies.
18. [In Press 2006b]. *La science dans les sociétés islamiques: approches historiques et perspectives d'avenir*. Edited by Mohammed Abattouy. Proceedings of the conference organized in Rabat, 16 et 17 avril 2004 (articles in Arabic, English and French). Casablanca: Publications of the King Abdulaziz Foundation for the Humanities and the Islamic Studies.
19. [In Press 2006c]. *L'Histoire des sciences arabes classiques: une bibliographie sélective commentée*. Casablanca: Publications of the King Abdulaziz Foundation for the Humanities and the Islamic Studies.
20. [Forthcoming 2006]. "Muʿassasat al-ʿūsba fī 'l-gharb al-islāmī fī ʿasr Ibn Khaldūn." Forthcoming in *Al-Abniya al-fikriya fī 'l-gharb al-islāmī zaman Ibn Khaldūn*. Proceedings of the meeting held in Marrakech in 23-26 February 2006. Rabat: The Faculty of Letters Press.
21. Abattouy, M., Renn, Jürgen, Weinig, Paul 2001. "Transmission as Transformation: The Translation Movements in the Medieval East and West in a Comparative Perspective." *Science in Context*, vol. 14: pp. 1- 12.
22. Aghayani Chavoshi, Jafar & Bancel, Faiza 2000. "Omar Khayyām et l'Hydrostatique." *Farhang. Quarterly Journal of Humanities and Cultural Studies* (Tehran) vol. 12: : pp. 33-49.
23. Anawati, Georges C. 1977. "Les divisions des sciences intellectuelles d'Avicenne." *Mélanges de l'Institut Dominicain d'Etudes Orientales du Caire* vol. 13: pp. 323-335.
24. Aristotle 1952. *Mechanica*. Greek text with English translation by E. S. Forster. In *The Works of Aristotle*, vol. 6: *Opuscula*. Oxford: Clarendon Press.
25. Bancel, Faiza 2001. "Les centres de gravité d'Abū Sahl al-Qūhī." *Arabic Science and Philosophy* vol. 11: pp. 45-78.
26. Bayhaqī, al-, ʿAlī ibn Zayd 1988. *Tārīkh ūkamāʿ al-islām*. Edited by M. Kurd ʿAlī. Damascus: Maʿbūʿat mujammaʿ al-lughā al-ʿarabiyya. Reprint of the 1st edition (1946).
27. Berggren, Lennart J. 1983. "The Correspondence of Abū Sahl al-Kūhī and Abū Isūʿq al-ʿĪbī. A Translation with Commentaries." *Journal for the History of Arabic Science* vol. 7: pp. 39-124.
28. Brown, Joseph Edward 1967. *The "Scientia de Ponderibus" in the Later Middle Ages*. Ph. D. Dissertation. Madison: The Wisconsin University Press.
29. Buchner, Franz 1922. "Die Schrift über den Qarastūn von Thabit b. Qurra." *Sitzungsberichte der Physikalisch-Medizinischen Sozietät zu Erlangen*. pp. 141-188.

30. Buckley, R. B. 1992. "The *Muútasib*." *Arabica* vol. 39: pp. 59-117.
31. Charette, François 2003. *Mathematical Instrumentation in Fourteenth-Century Egypt and Syria. The Illustrated Treatise of Najm al-Dīn al-Miṣrī*. Leiden: Brill.
32. Clagett, Marshall 1959. *The Science of Mechanics in the Middle Ages*. Madison: University of Wisconsin Press.
33. Damerow, Peter, Renn, Jürgen, Rieger, Simone, and Weinig, Paul 2002. "Mechanical Knowledge and Pompeian Balances." *Homo Faber: Studies on Nature, Technology, and Science at the Time of Pompeii*. Edited by Jürgen Renn and Giuseppe Castagnetti. Roma: L'Erma, pp. 93-108.
34. Dozy, R. 1927. *Supplément aux dictionnaires arabes*. Leiden: E. J. Brill, 2 vols.
35. Fūrībī, al-, Abū Naṣr Muáammad 1949. *úṣūl al-úlm*. Edited by Úthmān Amīn. Cairo: Dūr al-fikr al-árabī, 2nd edition.
36. Ghazālī, al-, al-Imām abū ūmid 1961. *Maqāṣid al-falāṣifa*. Edited by Sulaymān Dunyā. Miṣr [Cairo]: Dūr al-maáarif.
37. Gundissalinus, Dominicus 1903. *De Divisione Philosophiae*. Herausgeben und philosophiegeschichtlich untersucht... von Dr. Ludwig Baur. *Beiträge zur Geschichte der Philosophie des Mittelalters*, 4.2-3. Munster: Druck und Verlag der Aschendorffschen Buchhandlung.
38. [Gundissalinus, D.] Domingo Gundisalvo 1932. *De Scientiis*. Texto latino establecido por el P. Manuel Alonso Alonso. Madrid-Granada: Imprensa y Editorial Maestre.
39. Hall, Robert A. 1981. "Al-Khāzinī." *Dictionary of Scientific Biography*. 16 vols. Edited by Charles Gillispie. New York: Scribners, vol. VII: pp. 335-351.
40. ūasan, al-, Aúmad Yúsuf 1976. *Taqī al-Dīn wa al-handasa al-mákkāniyya al-árabīyya. Maáa 'Kitāb al-úruq al-saniyya fī al-áḥadīth al-rúḥniyya' min al-qarn as-sádis áshar*. Aleppo: Institute for the History of Arabic Science.
41. 1979. *Ibn al-Razzāz al-Jazarī: Al-Jāmiá bayna al-úlm wa al-ámal al-nāfiá fī ṣināat al-úyyal*. Aleppo: Institute for the History of Arabic Science.
42. 1981. *Banū Māsā: Kitāb al-úyyal*. Aleppo: Institute for the History of Arabic Science.
43. Heron von Alexandria 1976. *Heronis Alexandrini Opera quae supersunt*. 5 vols; vol. 2: *Mechanica et catoprica*. Edited by L. Nix and W. Schmidt. Stuttgart: B. G. Teubner. Reprint of the 1st edit. Leipzig: 1899-1914.
44. Héron d'Alexandrie 1988. *Les Mécaniques ou l'élevateur des corps lourds*. Texte arabe de Qusā ibn Lúqā établi et traduit par B. Carra de Vaux, Introduction de D. R. Hill et commentaires par A. G. Drachmann. Paris: Les Belles Lettres.
45. Heinen, Anton 1983. "At the Roots of the Medieval Science of Weights: A Report on an Edition Project." *The Journal of Sophia Asian Studies* (Tokyo) vol. 1: pp. 44-55.
46. Hill, Donald R. 1974. *The Book of Knowledge of Ingenious Mechanical Devices. An Annotated Translation of al-Jazarī's Treatise*. Dordrecht: Reidel.
47. 1979. *The Book of Ingenious Devices. An Annotated Translation of the Treatise of Banū Māsā*. Dordrecht: Reidel.
48. Hugonnard-Roche, Henri 1984. "La classification des sciences de Gundissalinus et l'influence d'Avicenne." *Etudes sur Avicenne*. Dirigées par J. Jolivet et R. Rashed. Paris: Les Belles Lettres, pp. 41-75.

49. Ibel, Thomas 1908. *Die Wage im Altertum und Mittelalter*. Erlangen: Junge (Erlangen Univ., Diss., 1906).
50. Ibn al-Akfln, Shams al-Dn 1989. *Kitāb Irshād al-qāṣid ilā asnā al-maqāṣid*. Edited by Junuarius Justus Withkam. Leiden: Ter Lugt Pers.
51. Ibn Snn, al-Shaykh al-Rāṣ ab ʿAlī 1331 H [1952]. *Miṣṣir al-uq ʿl, tasnif Shaykh Rāṣ ab ʿAlī Snn*. Persian text edited with introduction and notes by Jalāl al-Dn ḥ umā. Tehran: Anjuman-i Asar-i Milli.
52. 1989. *Tisā Rasāʿl fi ʿl-ūikma wa ʿl-abʿiyyat*. Cairo: Dār al-Bustān, 2nd edition.
53. Ibn al-Ukhuwwa, Muammad 1938. *The Maʿlim al-qurba fī aūkEm al-ūsba*. Edited, with abstract of contents, glossary and indices by Reuben Levy. Cambridge: Cambridge University Press/London: Luzac & Co.
54. Izzi Dien, Mawil 1997. *The theory and the practice of market law in medieval Islam. A study of Kitāb Nisab al-lūtisEb of ʿUmar b. Muammad al-SunEm (fl. 7th-8th/13th-14th century)*. Cambridge: E.J.W. Gibb Memorial Trust.
55. Jackson, David E. P. 1970. *The Arabic Version of the Mathematical Collection of Pappus Alexandrinus Book VIII*. Ph. D. Dissertation. University of Cambridge.
56. Jaouiche, Khalil. 1976. *Le Livre du qarāṣ ʿn de Thābit ibn Qurra. Etude sur l'origine de la notion de travail et du calcul du moment statique d'une barre homogène*. Leiden: Brill.
57. Jawbar, al-, ʿAbd al-Rāum 1979-80. *Le voile arraché. L'autre visage de l'Islam*. Traduction intégrale sur les manuscrits originaux par René Khawam 2 vols. Paris: Phébus.
58. Khāzin, al-, ʿAbd al-Rāum 1940 [1359 H]. *Kitāb mʿzEn al-ūikma*. Hyderabad: Dīrat al-maʿrif al-uthmāniyya.
59. King, David A. 1987. "The Astronomical Instruments of Ibn al-Sarrāj: A Brief Survey." In D. A. King, *Islamic Astronomical Instruments*. London: Variorum, B IX.
60. Knorr, Wilbur R. 1982. *Ancient Sources of the Medieval Tradition of Mechanics: Greek, Arabic and Latin Studies of the Balance*. Firenze: Istituto e Museo di Storia della Scienza.
61. Khwārizmī, al-, Ab ʿAbdallāh b. Y ʿsuf 1968. *Liber Mafatih al-Ouloum*. Edited by G. Van Vloten, Leiden: E. J. Brill, 2nd edition.
62. Lamrabet, Driss 2002. "Ibn Rashīq (XIII^{ème} siècle) et la classification des sciences mathématiques." In *Science et pensée scientifique en Occident musulman au moyen-âge*. Rabat: Publications de la Faculté des Lettres, pp. 43-56.
63. Lane, Edward W. 1984. *Arabic-English Lexicon*. 2 vols. Cambridge: The Islamic Texts Society.
64. Moody, Ernst, and Clagett, Marshall 1952. *The Medieval Science of Weights (Scientia de Ponderibus). Treatises ascribed to Euclid, Archimedes, Thabit ibn Qurra, Jordanus and Blasius of Parma*. Madison: The University of Wisconsin Press.
65. Philon de Byzance 1902. *Le livre des appareils pneumatiques et des machines hydrauliques*. Paris: C. Klincksieck.
66. Rozhanskaya, Mariam M. 1996. "Statics." In *Encyclopaedia of the History of Arabic Science*. 3 vols. Edited by R. Rashed. London: Routledge, vol. III, pp. 614-642.
67. ʿabū, al-, ḥ ussah al-SElim (supervision) 1989. *Al-ʿUl ʿm ʿinda al-ʿArab wa-al-Muslimn*. Collection of Dār

al- thĒr al-IslĒmiyya. Kuwait: DĒr al- thĒr al-IslĒmiyya.

68. SaġdĒn, Aġmad S. 1981. "Al-Umawġ." *Dictionary of Scientific Biography*. Vol. 13/14, pp. 539-540.
69. Saliba, George 1985. "The Function of Mechanical Devices in Medieval Islamic Society." *Science and Technology in Medieval Society*. Edited by Pamela Long. *Annals of the New York Academy of Sciences*, vol. 441: pp. 141-151.
70. Sbath, Paul, 1938-1940. *Al-Fihris: Catalogue des Manuscrits Arabes*. 3 parts plus Supplement. Cairo.
71. Sezgin, Fuat 1974. *Geschichte des Arabischen Schrifttums*. Vol. V: *Mathematik*. Leiden: E. J. Brill.
72. Shayzarġ, al-, Abd al-RaġmĒn b. Naġr 1999. *The Book of the Islamic Market Inspector. NihĒyat al-rutba fġ ħalab al-ġisba* (The utmost authority in the pursuit of *ġisba*). Translated with an introduction and notes by R. P. Buckley. Oxford: Oxford University Press.
73. TahĒnawġ, al-, Muġammad. [1862] 1988. *KashshĒf iġġilĒġĒt al-funġn*. *A Dictionary of the Technical Terms Used in the Sciences of the Musalmans*. 2 vols. Edited by M. Wajġh et al., Calcutta: W. N. Lees' Press. Reprinted Osnabrġck: Biblio Verlag.
74. Taylor, Jerome 1991. *The Didascalicon of Hugh de saint Victor. A Medieval Guide to Arts*. New York: Columbia University Press.
75. Wiedemann, Eilhard. 1970. *Aufsätze zur Arabischen Wissenschaftsgeschichte*. 2 vols. Hildesheim/New York: G. Olms.
76. ZiyġĒda, NġqġĒ 1962. *Al-ġ isba wa-'l-muġtasib fġ 'l-islĒm*. Beirut: al-Maġbaġ al-kĒthġrġkiyya.
77. Zotenberg H. 1879. "Traduction arabe du *Traité des corps flottants* d'Archimède." *Journal asiatique* vol. 7: pp. 509-515.